

It is perhaps easier to consider the cards as being in a fixed order and the counting to be a randomization of the given sequence (18 ones, 17 twos, 17 threes).

The number of sequences is $\frac{52!}{18!17!17!} = 99,579,591,790,845,629,463,000$.

Suppose that i ones, j twos and k threes are in specified positions with the same labels (forbidden positions).

The number of such sequences is $P(i, j, k) = \binom{4}{i} \binom{4}{j} \binom{4}{k} \frac{(52-i-j-k)!}{(18-i)!(17-j)!(17-k)!}$.

By the principle of inclusion-exclusion, the number of winning sequences is

$$\begin{aligned} & \sum_{i=0}^4 \sum_{j=0}^4 \sum_{k=0}^4 \binom{4}{i} \binom{4}{j} \binom{4}{k} \frac{(52-i-j-k)!}{(18-i)!(17-j)!(17-k)!} (-1)^{i+j+k} \\ &= 813,069,712,393,655,972,160, \end{aligned}$$

and the probability of winning is

$$\begin{aligned} & \left(\frac{52!}{18!17!17!} \right)^{-1} \sum_{i=0}^4 \sum_{j=0}^4 \sum_{k=0}^4 \binom{4}{i} \binom{4}{j} \binom{4}{k} \frac{(52-i-j-k)!}{(18-i)!(17-j)!(17-k)!} (-1)^{i+j+k} \\ &= \frac{24,532,967,512}{3,004,641,364,725} \approx 0.008165 \end{aligned}$$